INTRODUCTION
The AD5933 and AD5934 are high precision impedance converter system solutions. The main difference between these two solutions is the maximum measurable frequency. This application note applies to both parts. The main blocks of the AD5933 and AD5934 are shown in Figure 1.

The impedance converter is a finite system and has some limitations. This application note only aims to explain the optimum setup for measurements.

IMPEDANCE MEASUREMENT BLOCKS
Impedance converters can be divided into three different blocks: a transmit stage, a receive stage, and a discrete Fourier transform (DFT) engine.

Transmit Stage
The DDS core and the high speed DAC generate a sine wave signal used to excite the impedance.

The output programmable gain amplifier (PGA) is used for conditioning the output signal. It can be configured in four user selectable excitation voltages.

Receive Stage
The receive stage consists of

- The transimpedance amplifier (TIA) that converts the current that crosses the impedance into voltage
- The input PGA that amplifies the TIA signal ×1 or ×5
- The ADC that samples the signal and fills the internal buffer (1024 points)

DFT Engine
The DFT engine processes the data and generates real (R) and imaginary (I) number components.

![Figure 1. AD5933/AD5934 Block Diagram](image)
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# REVISION HISTORY

11/13—Revision 0: Initial Version
GETTING STARTED

BENEFITS OF ADDING AN EXTERNAL AFE

CN-217 describes an external analog front end (AFE) designed to improve measurements.

This AFE has two main benefits: to reduce the output impedance of the signal source and to rebias the excitation voltage signal.

REBIASING THE DC LEVEL

When connecting the impedance between $V_{IN}$ and $V_{OUT}$, as shown in Figure 2, notice that the dc bias voltage is slightly different in the transmit stage and receive stage.

The receiver dc offset is set to the ADC midscale, noninverting pin of the TIA, $V_{DD}/2$, while the dc offset in the transmitter depends on the selected output voltage shown in Table 1.

An example of the different dc bias voltages is shown Figure 3 for Range 1 where $V_{DD} = 5$ V.

Due to this mismatch, the dc level difference is amplified by the $R_{FB}$, or, in other words, the ADC dynamic range is reduced.

Additionally, a dc voltage across a sensor can polarize it and/or degrade it over the sensor lifetime.

REDUCING THE OUTPUT IMPEDANCE

The internal output impedance depends on the amplitude voltage range selected and this may be as high as 2.4 kΩ.

Therefore, since impedance cannot be considered negligible, it needs to be added into the equation. Typical values are shown in Table 2.

<table>
<thead>
<tr>
<th>Table 2. System Output Impedance</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Range No.</strong></td>
</tr>
<tr>
<td>1 to 4 (Adding external op amp)</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>4</td>
</tr>
</tbody>
</table>

The receiver dc offset is set to the ADC midscale, noninverting pin of the TIA, $V_{DD}/2$, while the dc offset in the transmitter depends on the selected output voltage shown in Table 1.

Table 1. DC Offset Voltage vs. Output Range for 3.3 V

<table>
<thead>
<tr>
<th>Range No.</th>
<th>DC Offset Voltage</th>
<th>V p-p</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.48</td>
<td>1.98</td>
</tr>
<tr>
<td>2</td>
<td>0.76</td>
<td>0.97</td>
</tr>
<tr>
<td>3</td>
<td>0.31</td>
<td>0.383</td>
</tr>
<tr>
<td>4</td>
<td>0.173</td>
<td>0.173</td>
</tr>
</tbody>
</table>
The total measurable impedance is the unknown impedance and the system output impedance. To measure small impedances, adding the system output impedance may dramatically increase the range thus increasing the total measurable impedance. Consequently, this reduces the output current. To compensate, the value of \( R_{FB} \) needs to increase. In other words, a high \( R_{FB} \) value means worse SNR and lower sensitivity in your system.

Implementing these suggestions is relatively easy. Rebiasing the dc level is straightforward; just add a high-pass filter. If you are planning to design the high-pass filter, refer to AN-581 Application Note, Biasing and Decoupling Op Amps in Single Supply Applications.

To reduce the output impedance and have the ability to measure low impedances, the recommended op amp of choice is the AD8606 (\( Z_{OUT} = 1 \Omega \)). You may consider the AD8602 as a lower cost alternative. Figure 4 shows the AFE implementation in the EVAL-AD5933EBZ, Rev. C1.

The second AD8606 is used as a TIA due to the lower leakage and noise; the internal receive stage TIA is operating as a voltage follower.

![Figure 4. AD5933 with AFE](image-url)
CONFIGURING THE PART

Correctly configuring the AD5933/AD5934 is key to getting the most accurate measurement from the part.

SELECTING THE EXCITATION VOLTAGE

The recommendation is to use the maximum output voltage because the SNR is degraded with lower amplitudes.

IDENTIFYING THE IMPEDANCE RANGE

The ratio between the maximum and minimum impedance is limited by the ADC resolution, supply, and dc offset for the selected range. The maximum ratio, \(Z_{\text{MAX}}/Z_{\text{MIN}}\), is shown in Table 3.

<table>
<thead>
<tr>
<th>DC Level</th>
<th>Range No.</th>
<th>Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rebiasing</td>
<td>1 to 4</td>
<td>×45</td>
</tr>
<tr>
<td>No Rebiasing</td>
<td>1</td>
<td>×40</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>×15</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>×5</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>×2</td>
</tr>
</tbody>
</table>

Remember to add the system output impedance into the impedance range. This depends on the selected range as shown in Table 2.

If the unknown impedance range does not fit within the maximum range, split your impedance range into subgroups. If this is the case, your system should be capable of changing the TIA gain. This can be done by adding an external mux or switch (that is, ADG1419) with different \(R_{\text{FB}}\) values as shown in Figure 5.

CHOOSING AN APPROPRIATE VALUE FOR \(R_{\text{FB}}\)

The internal ADC reference is \(V_{\text{DD}}\). It is important to guarantee that, in the worst case, the voltage generated by the TIA does not saturate the converter. The \(R_{\text{FB}}\) value is defined as

\[
R_{\text{FB}} = \left(\frac{V_{\text{DD}}}{2} - 0.2\right) \times Z_{\text{MIN}} \times \frac{1}{GAIN} - \frac{V_{\text{DCOFFSET}}}{2}
\]

where:

- \(V_{\text{PK}}\) is the peak voltage of the selected output range.
- \(Z_{\text{MIN}}\) is the minimum impedance.
- \(GAIN\) is the selected PGA gain, ×1 or ×5.
- \(V_{\text{DD}}\) is the supply.
- \(V_{\text{DCOFFSET}}\) is the dc offset voltage for the selected range shown in Table 1.

Note that if you are rebiasing, the signal \(V_{\text{DCOFFSET}}\) is \(V_{\text{DD}}/2\).

At this point, it is important to clarify that the equations are based on a headroom of 200 mV below \(V_{\text{DD}}\).

CHOOSING AN APPROPRIATE SETTLING TIME

The part allows preexcitation of the impedance before beginning measurements. This is recommended if the imaginary part of the load is bigger than the real part or if the distance sensor load is high. The settling time is referred to as the actual output frequency. Therefore, if you are generating a frequency sweep, the delay is different for each excitation frequency.

CALCULATING THE GAIN FACTOR

To calculate the gain factor, it is always recommended to use a discrete resistor rather than a complex impedance.

The reason for calibrating the system with a discrete resistor is simple. The algorithm to calculate the phase is relative, in other words, the unknown impedance phase is the difference between the calibrated phase minus the unknown measured phase. Therefore, to avoid confusion, it is necessary to calibrate the part using a zero phase delay impedance. The recommended impedance value for calibration is

\[
R_{\text{CAL}} = (Z_{\text{MIN}} + Z_{\text{MAX}}) \times \frac{1}{3}
\]

Recommendation

Regardless of how one wants to calculate the gain factor, it is always recommended to measure the system phase for each frequency because a typical op amp phase is not constant for some frequencies as shown in the example in Figure 6.

There are different ways to calculate the gain factor depending on the frequency range and memory space constrains.
Calculating the Gain Factor Using Single Impedance and Single Frequency

The impedance is excited with a single frequency. Typically, this is a frequency in the middle of your frequency sweep. This type of calibration is fast and requires minimum space in memory, but offers less precision than other methods. Specifically, the AD5933 DFT engine uses a method called single point DFT. Rather than analyze the entire spectrum and calculate the energy for a given frequency, the algorithm returns a single bin that contains multiple frequencies, at approximately 976.56 Hz at 1MSPS.

For example, when configuring a measurement for a 1 kHz excitation signal, the bin will contain the energy stored from 976 Hz to 1952 Hz.

On the board, there are many devices generating noise at different frequencies, such as an SMPS regulator; this could add more energy to the bin that the energy measured only in the impedance.

Calculating the Gain Factor Using Multipoint Frequencies, Single Impedance

In this case, calculate the gain factor for each frequency. This method is preferred if your frequency span is wide because it helps to reduce errors related to the op amp bandwidth as well as reducing bin errors.

There are two different ways to implement this method. The first way is to generate a look-up table in your controller for the gain factor. The second way is to calculate the gain factor on-the-fly by adding an external mux/switch as shown in Figure 7.

It is necessary to generate a sweep and repeat the measurement twice, once with R_CAL and a second time with the impedance (Z(ω)).

Improvements: Best Fit Equation

This is a method to correct offset and gain errors in the system, in other words, to linearize the system within a range.

First, the gain factor is calculated using one of the methods described in this application note.

Once the gain factor is calculated, measure the impedance in the extremes of the range as shown in Table 7.

The equations to correct the measured value are

\[ Z = M \times X + C \]
\[ M = \frac{(Z_{MAX} - Z_{MIN})}{(X_{MAX} - X_{MIN})} \]
\[ C = Z_{MIN} - (M \times X_{MIN}) \]

where:

- \( Z_{MAX} \) is the real maximum impedance.
- \( Z_{MIN} \) is the real minimum impedance.
- \( X_{MAX} \) is the maximum measured impedance.
- \( X_{MIN} \) is the minimum measured impedance.

The best fit equation for each frequency can be calculated, but this increases memory requirements.
WHEN THE IMPEDANCE IS OUTSIDE THE MAXIMUM AD5933/AD5934 MEASURABLE RANGE

There are some limitations in terms of maximum and minimum measurable impedance. In this case, the easy way to overcome the limitation is by adding a series or parallel resistance to decrease or increase the impedance as needed. This method decreases the accuracy because the unknown impedance is measured artificially in a different range.

EXAMPLE

Consider a simple example that works for several scenarios, where \( V_{DD} = 3.3 \text{ V} \).

In this case condition, the unknown impedance range is from 4.7 kΩ to 47 kΩ. Because the AD5933 measures impedance, not capacitance or inductance, calculate the equivalent impedance for your maximum and minimum excitation frequency (see Table 7).

As shown in Table 4, only Range 1 and Range 2 can be used for the measurements; all four ranges can be used if an external buffer is added. For this example, the selected op amp is the AD8606 as shown in CN-217.

Table 4. Selecting Ranges

<table>
<thead>
<tr>
<th>AFE</th>
<th>Range No.</th>
<th>Within Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Using AD8606</td>
<td>1 to 4</td>
<td>Yes</td>
</tr>
<tr>
<td>Without AFE</td>
<td>1</td>
<td>Yes</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>Yes</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>No</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>No</td>
</tr>
</tbody>
</table>

Calculate \( Z_{MIN} \) and \( Z_{MAX} \) according to Table 5.

Table 5. Maximum and Minimum Impedance to Measure

<table>
<thead>
<tr>
<th>With AFE</th>
<th>Without AFE</th>
</tr>
</thead>
<tbody>
<tr>
<td>AD8606</td>
<td></td>
</tr>
<tr>
<td>Range 1</td>
<td>( Z_{MIN}, 4.7 \text{ kΩ} )</td>
</tr>
<tr>
<td></td>
<td>( Z_{MAX}, 47 \text{ kΩ} )</td>
</tr>
</tbody>
</table>

Calculate \( R_{FB} \) according to Table 6.

Table 6. \( R_{FB} \) Values for Different PGA Configurations

<table>
<thead>
<tr>
<th>With AFE</th>
<th>Without AFE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Range 1</td>
<td>( x1, 6.8 \text{ kΩ} )</td>
</tr>
<tr>
<td></td>
<td>( x5, 1.4 \text{ kΩ} )</td>
</tr>
</tbody>
</table>

Calibrate the system, using

\[
R_{CAL} = \left( Z_{MIN} + Z_{MAX} \right) \times \frac{1}{3} = 17 \text{ kΩ}
\]

To analyze the results, note the performance results using multipoint calibration.

As shown in Figure 9 through Figure 12, the results without the AFE are slightly worse than those with an AFE. In all cases, the results are below the 1% except for Range 2 at low impedance.

In this case, the error is due to an assumption; the output impedance is 2.4. Figure 10 shows the error assuming that the output impedance is 2.4 ± 5%. To be considered negligible, the error added by the output impedance tolerance, \( Z_{MIN} \), should be at least 10 times larger than the amplifier output impedance.
If the system does not add an external buffer, there is a slight improvement using ×5 gain as shown in Figure 12.

![Figure 12. Error With and Without Gain Stage Enabled](image)

The difference is appreciable using Range 2 for 4.7 kΩ. The reason behind this surprising result is the noise. The amplifier noise is roughly estimated as

$$n_{\text{TOTAL}} = n_{\text{TIA}} + n_{\text{GAIN}}$$

$$n_{\text{TIA}} = \sqrt{(Z_{\text{UNKNOWN}} \times \text{GAIN})^2 + R_{\text{FB}}^2}$$

The equations intentionally omit the bandwidth contribution and other noise sources added by the op amp itself.

The PGA stage noise is constant while the TIA noise depends directly on the TIA gain. The worst case scenario is at maximum gain, $Z_{\text{LOAD}} = Z_{\text{MIN}}$.

**MEASURING A COMPLEX IMPEDANCE**

To measure complex impedance, refer to the conversion table (see Table 7) to calculate the maximum and minimum impedance based on the excitation frequency. This section describes three points to keep in mind.

**Do Not Calibrate the System with a Complex Impedance**

Otherwise, phase results will be not as expected. This is explained in the Calculating the Gain Factor section.

**There is a Minimum Excitation Frequency**

The ADC samples at MCLK/16 with a 1 MSPS maximum data rate. For an excitation frequency below 1 kHz sampling at the maximum data rate, the internal 1024-point buffer cannot store a full period; this adds a considerable error to the final result.

If you need to measure below 1 kHz, the recommendation is to reduce the MCLK frequency. This increases the calculation time; the DFT engine clock is MCLK and requires an external filter to attenuate harmonics. Keep the Nyquist theorem in mind since the internal filters are optimized for the maximum sample rate of 1 MSPS. For example, to measure the impedance at 10 Hz, MCLK = 16 MHz/100 = 160 kHz

**Inductance Can Be Measured**

The examples found in the data sheet are based on capacitors, but there are no restrictions or reasons why you cannot measure an inductor.

**MEASURING LIQUID**

To measure liquid, buy a commercial sensor or design your own. A sensor for this purpose typically has one or more parallel plates, rings, or nets as shown in Figure 13.

![Figure 13. Example of Sensor to Measure Liquids](image)

The measured impedance is defined by

$$Z = \frac{l}{A}\rho$$

where:

- $l$ is the distance between plates (or traces).
- $A$ is the area of the plates.
- $\rho$ is the electric resistivity.

The conductivity of a liquid is defined as

$$\sigma = \frac{1}{\rho}$$

The parameters of the sensor are constant, thus the impedance changes are driven by the electric conductivity.
SETTING UP AND PROGRAMMING

SETTING UP THE PART

Programming the part is a multistep process. Begin by setting up the part as follows:

- Internal oscillator: \( MCLK = 16.776\, \text{MHz} \)
- \( f_{\text{START}} = 1950\, \text{Hz} \)
- \( \Delta f = 975\, \text{Hz} \)
- Increments = 10
- PGA gain = \( \times 1 \)
- Output range = 2 V p-p
- Settling time = 1 ms worst case

PROGRAMMING THE PART

Once the part is set up, follow Step 1 through Step 7 to program the part.

1. **Reset the part.**
   - Write 0x10 to Register Address 0x81
2. **Program the start frequency.**
   \[
   D = \left( \frac{1950\, \text{kHz}}{16.776\, \text{MHz} \div 4} \right) \times 2^{27} = 0\times00F3C5
   \]
   - Write 0x00 to Register Address 0x82
   - Write 0xF3 to Register Address 0x83
   - Write 0xC5 to Register Address 0x84
3. **Program \( \Delta f \).**
   \[
   D = \left( \frac{975\, \text{Hz}}{16.776\, \text{MHz} \div 4} \right) \times 2^{27} = 0\times0079E2
   \]
   - Write 0x00 to Register Address 0x85
   - Write 0x79 to Register Address 0x86
   - Write 0xE2 to Register Address 0x87
4. **Program the number of increments.**
   - Write 0x00 to Register Address 0x88
   - Write 0x0A to Register Address 0x89
5. **Program the delay in the measurements.** The worst case is at maximum frequency, \( f_{\text{MAX}} = 1950 + (975 \times 10) = 11700\, \text{Hz} \)
   \[
   D = 1\, \text{ms} \times 11700 = 12
   \]
   - Write 0x00 to Register Address 0x8A
   - Write 0x0C to Register Address 0x8B
6. **Initialize the system.**
   - Write 0x11 to Register Address: 0x80
   - Wait several milliseconds.
7. **Follow the flowchart in Figure 14 to sweep the frequency.**
   If you need a new sweep, it is not necessary to reset the part again. Simply place the part in standby mode and program the registers again.
   - Write 0x30 to Register Address: 0x80
START FREQUENCY SWEEP
REGISTER ADDRESS: 0x80
DATA: 0x21

READ STATUS REGISTER
REGISTER ADDRESS: 0x8F

STATUS REGISTER [DATA AND 0x02] > 0

READ RESULT
REGISTER ADDRESSES, 0x94
0x95
0x96
0x97

DO YOU WANT TO AVERAGE THE MEASUREMENTS?
--AVERAGE; AVERAGE== 0

READ STATUS REGISTER
REGISTER ADDRESS: 0x8F

STATUS REGISTER [DATA AND 0x02] > 0

DONE
POWER DOWN THE PART
REGISTER ADDRESS: 0x80
DATA: 0xA0

REPEAT THE MEASUREMENT
REGISTER ADDRESS: 0x80
DATA: 0x41

GENERATE NEXT FREQUENCY
REGISTER ADDRESS: 0x80
DATA: 0x31

Figure 14. Flowchart
### Table 7. Example of Impedance Conversion

<table>
<thead>
<tr>
<th>Schematic</th>
<th>Impedance</th>
<th>Phase</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_R = R)</td>
<td>(\tan^{-1} \frac{0}{R} = 0)</td>
<td>Constant impedance</td>
</tr>
<tr>
<td><img src="C" alt="C" /></td>
<td>(Z_C = \frac{1}{Cwj})</td>
<td>(-\tan^{-1} \left(\frac{Cw}{0}\right) = -\frac{\pi}{2})</td>
<td>Use higher capacitance to calculate the lowest impedance and minimum capacitance value to calculate highest impedance</td>
</tr>
<tr>
<td><img src="L" alt="L" /></td>
<td>(Z_L = Lw)</td>
<td>(\tan^{-1}(Lw) = \frac{\pi}{2})</td>
<td>Use lower inductor to calculate the lowest impedance and maximum inductor value to calculate highest impedance</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(\frac{1}{Z_T} = \frac{1}{Z_R} + \frac{1}{Z_C} = \frac{1}{Y_T})</td>
<td>(\tan^{-1} \left(\frac{0}{R}\right) - \tan^{-1} \frac{RCw}{1})</td>
<td>(= -\tan^{-1} RCw)</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Y_T = \frac{1}{R} + \frac{Cw}{R} = \frac{1 + RCw}{R})</td>
<td>(\frac{R}{1 + RCw})</td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = \frac{R}{1 + RCw})</td>
<td></td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMAX}</td>
<td>= \frac{R}{\sqrt{1^2 + (2\pi R C f_{MIN})^2}})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMIN}</td>
<td>= \frac{R}{\sqrt{1^2 + (2\pi R C f_{MAX})^2}})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = Z_R + Z_C)</td>
<td>(\tan^{-1} \frac{RCw}{1} - \tan^{-1} \frac{Cw}{0})</td>
<td>(= -\tan^{-1} RCw - \frac{\pi}{2})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = R + \frac{1}{Cw} = \frac{1 + RCw}{Cwj})</td>
<td></td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMAX}</td>
<td>= \frac{\sqrt{1^2 + (2\pi R C f_{MIN})^2}}{2\pi R C f_{MIN}})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMIN}</td>
<td>= \frac{\sqrt{1^2 + (2\pi R C f_{MAX})^2}}{2\pi R C f_{MAX}})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = Z_R + Z_L)</td>
<td>(\tan^{-1} \frac{Lw}{R})</td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = R + Lwj)</td>
<td></td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMAX}</td>
<td>= \sqrt{R^2 + (2\pi L f_{MAX})^2})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(</td>
<td>Z_{TMIN}</td>
<td>= \sqrt{R^2 + (2\pi L f_{MIN})^2})</td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = \frac{R}{1 + RCw} + Lwj)</td>
<td></td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = -RLCw^2 + Lwj + R)</td>
<td></td>
<td></td>
</tr>
<tr>
<td><img src="R" alt="R" /></td>
<td>(Z_T = \frac{Lw}{R} - RLCw^2 - \tan^{-1} \frac{RCw}{1})</td>
<td></td>
<td>(j = \sqrt{-1}) (j^2 = -1)</td>
</tr>
</tbody>
</table>